

Elastic and mechanical properties of cubic metal arsenides (Ga, In and Al) under high-pressure: a simulation study

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Received: 26th March 2020, Revised: 6th June 2021, Accepted: 19th June 2021

Abstract Semiconducting materials have played an important role in modern technological age. Group III-V materials have attracted much attention in electronic industry due to their structural, mechanical, electronic and thermodynamic properties predicted by calculations. This paper simulated the effect of pressure within the range of 0-100 GPa on the elastic constants and other related parameters, such as Young's, bulk and shear moduli, Pugh ratio, Poisson ratio, anisotropy factor, degree of anisotropy and Kleinman parameter for gallium arsenide (GaAs), indium arsenide (InAs) and aluminum arsenide (AlAs) materials, using the Tersoff classical potential within ATK-force field. Results showed that, increase in pressure enhanced the ductility of GaAs and InAs within the entire pressure domain, and between 10-40 GPa for AlAs material. AlAs was found to be brittle under 50-90 GPa, and unstable at 100 GPa. This may be due to occurrence of phase transition at these pressures. The obtained results at zero pressure are consistent with available experimental and theoretical data in literature.

Keywords: Elastic constants, ductility, gallium arsenide, high pressure, indium arsenide.

1 Introduction

The knowledge of high-pressure dependence of the elastic parameters is critical for predicting some physics of semiconducting materials. For instance, high-pressure analysis gives vital information about the phase transition, stability, strength, elastic, and mechanical properties of semiconductors (Liu *et al.* 2007, Zhu *et al.* 2008, Liu *et al.* 2009, Wang *et al.* 2009, Guler and Guler 2014). Currently, III-V compound semiconductors, such as gallium arsenide (GaAs), indium arsenide (InAs) and aluminum arsenide (AlAs) are the major materials for micro/nano/opto-electronic

device applications. They exhibit excellent optical, elastic, mechanical, and electronic properties which make them suitable for applications and have received considerable interest from experimental and theoretical researchers. GaAs is used in photovoltaics, semiconductor lasers, light emitting diodes, solar cells and heterostructures (Blakemore 1982, Rong *et al.* 2008, Al-Douri and Ali 2011). AlAs is used in high electric mobility transistors, solid state lasers, Bragg reflector super lattices and heterojunction bipolar transistors (Liu 1995, Li *et al.* 2013), and InAs is used in infrared detectors, photodiodes, and terahertz radiation source (Lide 1998).

Elastic parameters provide connection between mechanical and dynamic property of cubic crystals and give insight into the nature of forces operating in materials. Under standard conditions, GaAs, InAs and AlAs crystallize in cubic zinc-blend structure. At high pressure, these materials are found to undergo structural phase transition, thereby exhibiting different mechanical properties. Phase transition and elasticity of GaAs was reported by Guller and Guller (2014) up to 25 GPa from Geometry Optimization technique. Li *et al.* (2013) reported the pressure dependence of elastic and lattice dynamics properties of AlAs from ab initio studies up to 15 GPa. Also, Kabita *et al.* (2016) studied structural, elastic, and electronic properties of InAs under induced pressure within the range of 0-4 GPa, and Louail *et al.* (2006) reported the elastic properties of InAs under pressure up to 18 GPa, using the CASTEP density functional theory.

Although, there have been studies on elastic and mechanical properties of these binary compounds under ambient conditions, experimental and theoretical investigations of these properties under high pressure are still scanty in literature. Therefore, the objective of this simulation work is to reveal the behaviour of elastic and mechanical properties of GaAs, InAs and AlAs under pressure in the range of 0 – 100 GPa.

2 Computational Methods

The computation of elastic parameters of GaAs, InAs and AlAs were performed using ATK-force field code with Tersoff potentials (Nordlund *et al.* 2000, Hammerschmidt *et al.* 2008, Fichthor *et al.* 2011) as implemented in QuantumATK under the framework of Virtual Nano Lab. In this method, QuantumATK employs the Lagrangian strain and stress tensors. The strain and stress tensors are defined by 3X3 matrices using the Voigt notation, and they can be written compactly as 6-vectors:

$$\begin{aligned}\sigma &= (\sigma_{xx}, \sigma_{yy}, \sigma_{zz}, \sigma_{xy}, \sigma_{xz}, \sigma_{yz}) \\ \varepsilon &= (\varepsilon_{xx}, \varepsilon_{yy}, \varepsilon_{zz}, \varepsilon_{xy}, \varepsilon_{xz}, \varepsilon_{yz})\end{aligned}\tag{1}$$

Usually, the linear response of the stress to a strain vector is given as

$$\sigma = C \cdot \varepsilon \quad (2)$$

The number of independent elements in matrix C can be reduced depending on the crystal symmetry. For example, triclinic, monoclinic, orthorhombic, tetragonal II, rhombohedral, and hexagonal crystals, respectively have 21, 13, 9, 7, 6 and 5 independent elastic constants. However, in cubic crystal system, only 3 elastic constants (C_{11} , C_{12} and C_{44}) are totally independent as given by equation 3 (Born 1940, Mouhat and Coudert 2014),

$$\begin{pmatrix} \sigma_1 \\ \sigma_2 \\ \sigma_3 \\ \sigma_4 \\ \sigma_5 \\ \sigma_6 \end{pmatrix} = \begin{pmatrix} C_{11} & C_{12} & C_{12} & 0 & 0 & 0 \\ C_{12} & C_{11} & C_{12} & 0 & 0 & 0 \\ C_{12} & C_{12} & C_{11} & 0 & 0 & 0 \\ 0 & 0 & 0 & C_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & C_{44} & 0 \\ 0 & 0 & 0 & 0 & 0 & C_{44} \end{pmatrix} \begin{pmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \varepsilon_3 \\ \varepsilon_4 \\ \varepsilon_5 \\ \varepsilon_6 \end{pmatrix} \quad (3)$$

where σ_i , ε_i and C_{ij} are stress, strain and stiffness constants, respectively. To calculate the stiffness constants C_{ij} , the atomic positions of each strained cell is first optimized. Then, QuantumATK (Atomistix ToolKit 2017.2) uses the universal linearly independent coupling strain (ULICS) vectors to minimize the number of stress calculations. For each strain vector three deformations ($-\eta$, 0, $+\eta$) centered at $\eta=0$, is applied to simulate the cell along selected strains and calculate the corresponding stress vectors. Here, we use $\eta=0.002$, and number of intermediate deformations $n_\eta=3$ to filter out possible non-linear contributions. The highest polynomial order was taken as one in the stress against η fitting. Contributions from the linear stress are obtained by fitting the stress $\sigma_i(\eta)$ curves of each Voigt stress and for every strain component. Then, taking crystal symmetry into account, the independent stiffness constants are calculated as the least-squares solution to a linear system of equations. The calculations were performed within a range of pressures, 0 – 100 GPa. Also, the code calculates the Poisson ratio, shear, bulk, and Young's modulus.

3 Results and Discussion

Elastic properties provide information about the dynamical and mechanical behavior of crystals and the nature of forces acting on the crystal. Mathematically, they are proportionality constants between stress and strain, which provides information on

the interatomic stability of the crystal (Pokluda *et al.* 2015). As a result, any change on the stress or strain within the crystal has direct effect on the elastic constants (C_{ij}). From the Born mechanical stability conditions for cubic structure, the elastic constants must satisfy the following necessary and sufficient conditions (Born 1940, Mouhat and Coudert 2014):

$$\begin{aligned} C_{11} - C_{12} > 0; \quad C_{44} > 0; \quad C_{11} + 2C_{12} > 0, \\ C_{12} < B < C_{11} \end{aligned} \quad (4)$$

The calculated values of C_{ij} for GaAs are listed in Table 1 along with experimental and theoretical results available in the literature (Blakemore 1982, Varshney *et al.* 2010, Guler and Guler 2014). Table 1 shows that the results of C_{ij} for GaAs agree with other theoretical results (Varshney *et al.* 2010) at 0 GPa. The calculated results for C_{11} , C_{12} and C_{14} satisfy the structural and cubic stability conditions in Eq. (4) for gallium arsenide, indicating that cubic GaAs is mechanically stable within the high-pressure regime (0 – 100 GPa).

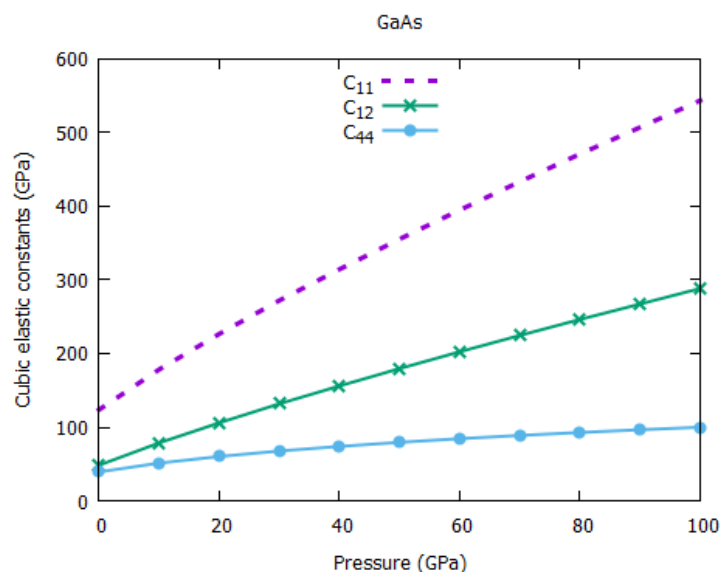


Fig. 1. The cubic elastic constants C_{11} , C_{12} and C_{14} for GaAs under pressure.

Figure 1 shows the stiffness constants at different pressures for GaAs. From these plots, all the calculated cubic stiffness constants are positive and increase monotonically as pressure increases. In addition, increase in C_{11} is higher than C_{12} and C_{14} . It is well known that C_{11} represents the longitudinal stiffness behavior, C_{12} represents the off-diagonal stiffness characteristics and C_{44} explains the shear

stiffness behavior of cubic crystals. As a result, longitudinal strain generates a change in volume without a corresponding change in shape. Therefore, this gives rise to larger change in C_{11} since volume is related to pressure. A transverse strain (or shearing) causes a change in shape without a corresponding change in volume. Therefore, C_{12} and C_{14} are less sensitive to pressure compared to C_{11} (Guler and Guler 2014).

The bulk modulus (B), shear modulus (G), Young's modulus (E), Pugh ratio (B/G), Poisson ratio (ν), Kleinman parameter (ζ) and Anisotropy factor A for GaAs at different pressures are listed in Table 1. The Young's modulus is defined as the ratio of stress to strain. It is the resistance to uniaxial tensions and is used to provide a measure of the stiffness of solids. This implies that, the higher the value of E, the stiffer the material. This trend agrees with previous studies (Bing *et al.* 2010, Feng *et al.* 2014, Wang *et al.* 2014).

Table 1: Calculated elastic constants C_{11} , C_{12} , C_{14} (GPa) and other related elastic parameters for GaAs at various pressure P (GPa). (B: bulk modulus (GPa), G: shear modulus (GPa), E: Young modulus (GPa), B/G: Pugh ratio, ν : Poisson ratio, ζ : Kleinman parameter, A: Anisotropy factor.

P	C_{11}	C_{12}	C_{14}	B	G	E	B/G	ν	ζ	A
0	123.61 (106.5 ^a) (106.5 ^b) (122.3- 147.6 ^c)	48.27 (53.3 ^a) (60.2 ^b) (40.6- 119 ^c)	39.14 (60.2 ^a) (33.6 ^b) (42.4- 107 ^c)	73.38 (75.5 ^a) (75.6 ^b) (70.8- 135 ^c)	38.54 (32.6 ^a) (28.9 ^b) (24.5 ^c)	96.49 (85.5 ^a) (63.0 ^b)	1.90	0.281 (0.31 ^a) (0.36 ^b)	0.530	1.039
10	178.29	78.62	51.13	111.84	50.60	130.16	2.21	0.306	0.574	1.026
20	226.52	105.84	60.09	146.06	60.18	159.10	2.42	0.319	0.597	0.995
30	272.02	131.76	67.55	178.51	68.57	186.03	2.60	0.326	0.611	0.963
40	314.29	155.97	73.80	208.74	75.90	210.83	2.75	0.332	0.621	0.932
50	355.30	179.54	79.34	238.12	82.65	234.76	2.88	0.336	0.629	0.902
60	394.86	202.33	84.26	266.50	88.68	257.75	3.00	0.339	0.635	0.875
70	433.37	224.57	88.71	294.16	94.68	280.07	3.10	0.341	0.640	0.849
80	470.86	246.23	92.74	321.11	100.12	301.76	3.20	0.343	0.644	0.825
90	507.08	267.18	96.38	347.14	105.20	322.68	3.29	0.345	0.647	0.803
100	543.52	288.27	99.82	373.35	110.14	343.71	3.38	0.347	0.650	0.782

^a Blakemore (1982), ^b Guler and Guler (2014), ^c Varshney *et al.* (2010)

It is clear from Table 1 that, pressure has significant effect on E. Thus, Young's modulus of GaAs shows a monotonic increase with pressure as displayed in Figure 2.

This means that GaAs is stiffer at higher pressures because the higher the value of Young's modulus, the harder the material.

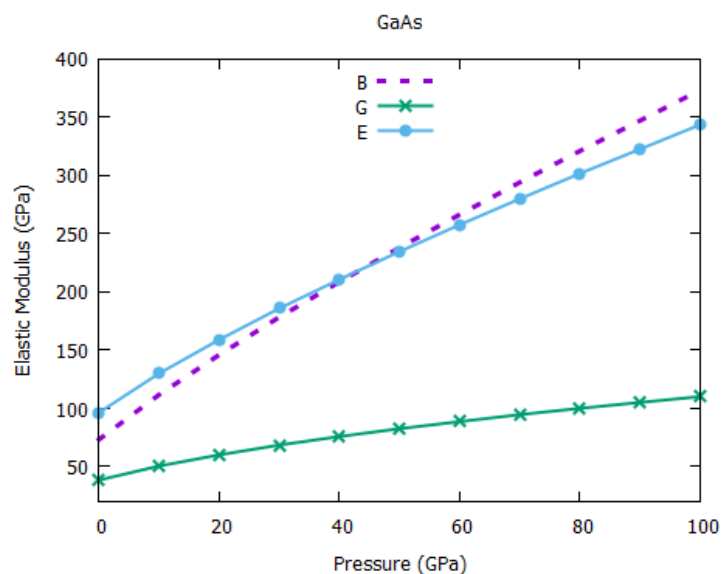


Fig. 2. Young, bulk, and shear modulus for GaAs under pressure.

Bulk modulus is defined as a measure of resistance to external deformation, and it gives a lot of information about bonding strength of materials (Bensalem *et al.* 2014, Guemou *et al.* 2014). Since pressure is directly proportional to bulk modulus, it is predictable that increase in pressure leads to corresponding increase in bulk modulus ($\Delta P = \Delta V \times B$). Results obtained for B as captured in Table 1 increase rapidly with pressure. As the pressure is increased from 0 to 100 GPa, the bulk modulus was observed to increase from 73.38 to 373.35 GPa as displayed in Figure 2. The value obtained at zero pressure is consistent with experimental and theoretical results (Blakemore 1982, Guler and Guler 2014). In addition, shear modulus is known to measure the resistance to change in shape created by a shearing force. Results obtained for G increased from 38.54 to 110.14 GPa as the pressure is increased from 0 to 100 GPa. This result at zero pressure is consistent with experimental result (Blakemore 1982). This means that increase in pressure improves GaAs resistance to change in shape due to shearing forces.

Mechanical properties of solid materials can be investigated by employing the empirical Pugh ratio (B/G) to determine if a material exhibits ductile or brittle behavior (Pugh 1954, Rahmati *et al.* 2014); i.e., if $B/G > 1.75$, the material behaves in a ductile manner, whereas, if $B/G < 1.75$ the material behaves in a brittle manner.

Figure 3(a) is a plot of Pugh ratio against pressure up to 100 GPa. Pugh ratio analysis shows the ductile nature of gallium arsenide under pressure. From our calculations, the value of Pugh ratio is higher than 1.75 and increases with pressure. Therefore, GaAs can be classified as a ductile material under pressure up to 100 GPa, and pressure improves the ductility of this material.

Poisson ratio is defined as the ratio between the transverse strain and longitudinal strain in the elastic loading direction. It is utilized to reveal the stability of materials against shear and provides information about the type of bonding forces (Cao *et al.* 2013, Greaves *et al.* 2013). The larger values of Poisson's ratio favours plasticity of a material. For covalent materials $\nu = 0.1$, ionic materials $\nu = 0.25$, and values between 0.25 to 0.5 signifies that a central force exist in the solid material. In this study, the Poisson's ratio begins with 0.281 at zero pressure and increased to 0.347 with applied pressure as displayed in Figure 3(b). This signifies that those central forces are predominant in GaAs material. This result is consistent with previous studies.

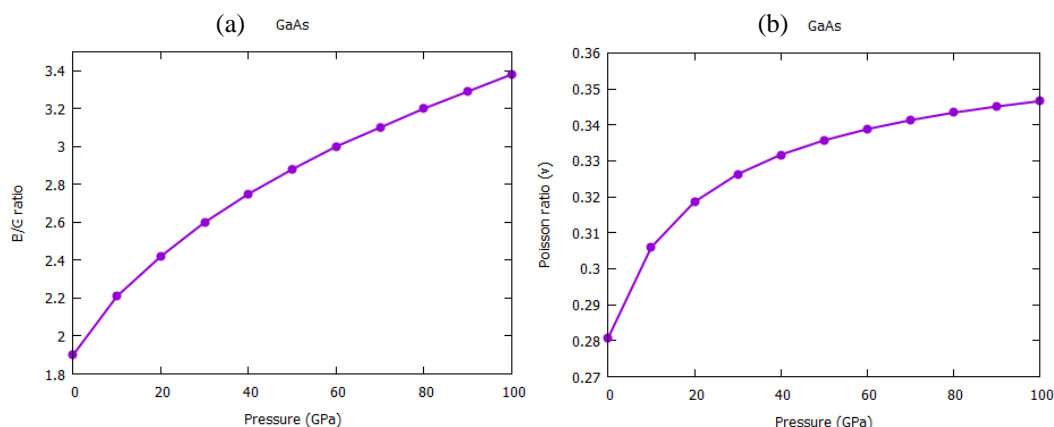


Fig. 3. (a) Pugh ratio (B/G) and (b) Poisson's ratio for GaAs under pressure.

Kleinman parameter (ζ) describes the relative positions of anion and cation sublattices under volume conserving strain distortions for which positions are not fixed by symmetry. According to Harrison (1989), it is given by the relation:

$$\zeta = \frac{C_{11} + 8C_{12}}{7C_{11} + 2C_{12}} \quad (5)$$

In a system, reducing bond stretching leads to $\zeta = 1$, while reducing bond bending leads to $\zeta = 0$. In this study, as the pressure increases, Kleinman parameter was observed to vary from 0.53 to 0.56, indicating a decrease in bond stretching for

GaAs. ζ grows monotonically with increase in pressure as shown in Figure 4(a), and increasing pressure reduces bond stretching.

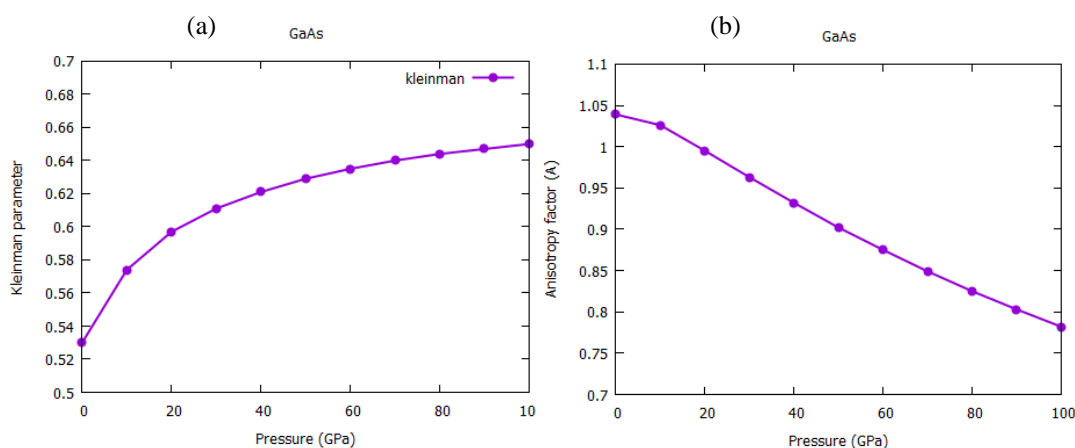


Fig. 4. (a) Kleinman parameter and (b) Anisotropy factor for GaAs under pressure.

Elastic anisotropy factor (A) gives vital information about the degree of anisotropy in solid materials (Zener 1948). It has potential to influence micro-cracks in materials; as such it has vital implications in material engineering. $A = 1$, implies the material under study is elastically isotropic and deform uniformly along all directions. Whereas, if $A > 1$, the material is stiffest along the $\langle 111 \rangle$ direction, and for $A < 1$, it is stiffest along $\langle 100 \rangle$ direction (Kabita *et al.* 2015). The value of A is calculated at various pressures using the following relation (Maachou *et al.* 2011):

$$A = \frac{2C_{44}}{C_{11} - C_{12}} \quad (6)$$

Figure 4(b) displays calculated values of A against applied pressure. It was observed that the anisotropy factors are not equal to one, rather decreased from 1.039 to 0.782 with increasing pressure. This implies that, between 0 – 10 GPa ($A > 1$) GaAs tends to be stiffest along $\langle 111 \rangle$ body diagonals, and between 20 – 100 GPa ($A < 1$) gallium arsenide tends to be stiffest along $\langle 100 \rangle$ cube axes.

The calculated elastic parameters for cubic indium arsenide under the effect of pressure up to 100 GPa have been listed in Table 2. The mechanical stability conditions in Eq. (4) can validate the calculated stiffness constants within the entire pressure domain, 0 – 100 GPa. The obtained results of elastic constants for InAs meet the stability conditions, indicating that they are mechanically stable at high-pressure.

The calculated results for elastic constants at 0 GPa are slightly higher than both experimental and theoretical values. This might be associated with the potential force field used in this calculation. However, this does not affect the validity of these results, since they are within the acceptable limits of calculations using different classical potential force field.

Table 2: Calculated elastic constants C_{11} , C_{12} , C_{44} (GPa) and other related elastic parameters for InAs at various pressure P (GPa). (B : bulk modulus (GPa), G : shear modulus (GPa), E : Young modulus (GPa), B/G : Pugh ratio, ν : Poisson ratio, ζ : Kleinman parameter, A : Anisotropy factor, A^* : degree of elastic anisotropy).

P	C_{11}	C_{12}	C_{44}	B	G	E	B/G	ν	ζ	A	$A^*(10^{-2})$
0	113.58 (83.29 ^b) (83.0 ^a) (84.1 ^c)	55.92 (45.26 ^b) (46.7 ^a) (48.1 ^c)	54.69 (39.59 ^b) (37.2 ^c)	75.13 (58 ^e) (71.85 ^c)	42.29	76.67	1.78	0.3299	0.6185	1.897	4.84
10	161.65	88.06	67.71	112.58	53.01	99.53	2.12	0.3527	0.6624	1.840	4.39
20	204.69	117.39	77.02	146.49	61.32	119.11	2.39	0.3645	0.6858	1.764	3.81
30	244.38	144.76	84.14	177.96	68.18	136.67	2.61	0.3720	0.7011	1.689	3.26
40	282.33	171.14	89.90	208.20	74.14	153.14	2.81	0.3774	0.7122	1.617	2.74
50	318.45	196.40	94.58	237.08	79.33	168.59	2.99	0.3815	0.7207	1.549	2.28
60	252.94	220.65	98.40	264.74	83.91	183.18	3.16	0.3847	0.7274	1.487	1.87
70	387.23	244.84	101.64	292.30	88.12	197.55	3.32	0.3874	0.7330	1.427	1.51
80	420.51	268.39	104.31	319.09	91.91	211.37	3.47	0.3896	0.7377	1.371	1.18
90	452.90	291.38	106.49	345.22	95.32	224.75	3.62	0.3915	0.7417	1.318	0.99
100	484.23	313.66	108.23	370.51	98.38	237.61	3.77	0.3931	0.7452	1.269	0.68

^aEllaway and Faux (2003), ^bGerlich (1963), ^cVictor *et al.* (2017), ^dHellwege *et al.* (1982)

Due to difficulty in measuring high pressure dependence of elastic parameters, there are no experimental values for InAs in the literature to compare with. Therefore, these results can be used as the basis for experimental work at high pressures for indium arsenide material. It is clear from Table 2 that, C_{11} , C_{12} and C_{44} increase with increasing pressure. Also, C_{11} is more sensitive to change in pressure compared to C_{12} and C_{44} . Results obtained for bulk modulus B at zero pressure is consistent with other theoretical studies (Victor *et al.* 2017). As the pressure is increased to 100 GPa, B was observed to increase rapidly to 370.51 GPa. This means that increase in pressure enhances the resistance to external deformation for InAs. Shear modulus G for InAs was observed to increase monotonically with pressure. This indicates that the higher the pressure the larger the value of G . Hence, InAs becomes more resistant to change in shape due to shearing forces at high pressure. In Table 2, one can observe that

Young's modulus E is sensitive to pressure. E increased from 76.67 to 237.61 GPa as applied pressure is increased from 0 to 100 GPa, meaning an increase in induced pressure improves the stiffness of indium arsenide, since Young's modulus is a measure of stiffness of solid materials. This implies that InAs becomes extremely hard to be broken at high-pressure. Pugh ratio B/G was observed to increase from 1.78 to 3.77 within the pressure range. Since $B/G > 1.75$, it means that indium arsenide behaves as a ductile material from low to high pressure regime, and the ductility of this material increases with pressure.

Poisson ratio ν for this material was observed to increase from 0.3299 to 0.3931 as induced pressure increases from 0 to 100 GPa. This indicates that central force exists in this material since $\nu > 0.25$, and Poisson ratio increases with pressure. This is consistent with Victor *et al.* (2017). The Kleinman parameter which determines bond bending and bond stretching was observed to be 0.6185 at zero pressure and 0.7452 at 100 GPa. This means that pressure reduces bond stretching in InAs, similar to our observation in gallium arsenide material. Furthermore, it was observed that elastic anisotropy factor A is not equal to one, indicating the existence of elastic anisotropy in InAs. From Table 2, increase in pressure reduces A from 1.897 to 1.269 for InAs. This means that InAs is stiffest along $\langle 111 \rangle$ body diagonals. For cubic crystals, the degree of elastic anisotropy (A^*) is calculated as $A^* = 3(A-1)^2 / (3(A-1)^2 + 25A)$ (Bing *et al.* 2010). In this study, A^* was found to decrease from 0.0484 to 0.0068 as induced pressure is increased from 0 to 100 GPa.

Table 3. Calculated elastic constants C_{11} , C_{12} , C_{14} and other related elastic parameters for AlAs at various pressure P . (B: bulk modulus, G : shear modulus, E : Young modulus, B/G : Pugh ratio, ν : Poisson ratio).

P (GPa)	C_{11} (GPa)	C_{12} (GPa)	C_{44} (GPa)	B (GPa)	G (GPa)	E (GPa)	B/G	ν
0	120.77 (120 ^a) (119 ^b) (116 ^c)	57.34 (58.2 ^a) (54.8 ^b) (55 ^c)	67.26 (57.6 ^a) (60.4 ^b) (57 ^c)	78.48	49.73	83.84	1.58	0.3220 (0.328 ^a)
10	170.37	90.81	83.27	117.33	61.90	107.21	1.89	0.3477
20	214.83	121.54	94.70	152.54	71.36	126.99	2.14	0.3613
30	255.92	150.37	103.95	185.55	79.18	144.60	2.34	0.3701
40	294.92	178.04	111.33	217.00	85.95	160.88	2.52	0.3764
50	64987.01	12078.70	31321.77	29714	29274.61	61200.76	1.01	0.1567
60	67358.46	7352.81	31996.50	27354.69	31183.54	65911.18	0.877	0.0948
70	67492.72	7067.77	32036.41	27209.41	31293.99	66152	0.869	0.0948
80	67625.79	6783.16	32076.41	27064.03	31403.79	66389	0.818	0.0912
90	67757.73	6498.87	32116.18	26918.49	31512.98	66620	0.854	0.0875
100	288.15	173.22	110.13	211.52	84.82	158.08	2.490	0.3754

^aGehrsitz *et al.* (1999), ^bLi *et al.* (2013), ^cChetty *et al.* (1989)

For AIAs, results obtained at zero pressure are in agreement with both experimental and theoretical values (Chetty *et al.* 1989, Gehrsitz *et al.* 1999, Li *et al.* 2013). All calculated elastic parameters increased with pressure up to 40 GPa (Table 3). Beyond this point, we observed a drastic jump in the values of C_{11} , C_{12} , C_{44} , B , G and E , and sudden drop in values of ν and B/G . This behavior was observed between 50 to 90 GPa. Again, at 100 GPa there was sudden drop in the values of C_{11} , C_{12} , C_{44} , B , G and E . Whereas, a jump in values of ν and B/G was observed. This behavior might be associated with phase transition that might have occurred at these respective pressures. It was observed experimentally that between 12.4 – 14.2 GPa, zincblende AIAs undergoes phase transition to nickel arsenide phase (NiAl-AIAs) (Foyen and Cohen 1983, Weinstein *et al.* 1987). Theoretically, it has been reported that at 77.9 GPa phase transition from NiAl-AIAs to CsCl-AIAs phase was observed (Mujica *et al.* 1995).

The calculated values of stiffness constants (C_{11} , C_{12} , C_{44}) and B modulus support both the structural and cubic stability conditions for AIAs within the pressure range 50 – 90 GPa. However, the cubic stability condition $C_{12} < B < C_{11}$ was violated since $C_{12} > B$ at 100 GPa. This might be as a result of phase transition to the unstable CsCl-AIAs phase at 100 GPa. This implies that AIAs becomes unstable at high pressure above 100 GPa. From our results, at zero pressure, 50, 60, 70, 80 and 90 GPa, Pugh ratio is less than 1.75. This suggests that AIAs is brittle at these pressures. Whereas, from 10 – 40 GPa and 100 GPa AIAs material shows ductile behavior. Additionally, Poisson's ratio for this material was observed to decrease as pressure increase from 50 to 90 GPa. Since Poisson's ratio suggests stability of crystal against shear deformation, larger values implies better plasticity. Therefore, between the pressures 0 – 40 GPa, AIAs show better plasticity behavior, and between 50 – 90 GPa, AIAs exhibits lesser plasticity.

5 Conclusions

This work has described the elastic and mechanical properties of GaAs, InAs and AIAs under high pressure up to 100 GPa. Results obtained at zero pressure are consistent with some of the experimental and theoretical values previously reported. According to the Born mechanical stability condition, GaAs and InAs are mechanically stable under the entire high-pressure region, while for AIAs the stability condition is violated at 100 GPa. Calculated Young, bulk and shear moduli, Poisson ratio, anisotropy factor, degree of anisotropy, Kleinman parameter and Pugh ratio indicated that the ductility of GaAs and InAs will be enhanced with pressure. The aluminum arsenide material was found to be brittle under 50 – 90 GPa and unstable at 100 GPa.

Acknowledgements

The authors acknowledge the Federal University of Petroleum Resources Effurun for providing the Mini Workstation used for the calculations and QuantumATK for access to the VNL-ATK software package. Also, we wish to acknowledge the two anonymous reviewers for their meaningful comments to make this manuscript better.

References

- Atomistix ToolKit 2017.2. Quantumwise A/S, www.quantumwise.com
- Bensalem S, Chegaar M, Maouche D, Bouhemadou A. 2014. Theoretical study of structural, elastic and thermodynamic properties of CZTX (X=S and Se) alloys. *Journal of Alloys and Compounds* 589: 137-142. doi.org/10.1016/j.jallcom.2013.11.113.
- Bing L, Rong-Feng L, Yong Y, Xiang-Dong Y. 2010. Characterisation of the high-pressure structural transition and elastic properties in boron arsenic. *Chinese Physics B* 19 (7): 076201. doi:10.1088/1674-1056/19/7/076201.
- Blakemore JS. 1982. Semiconducting and other major properties of gallium arsenide. *Journal of Applied Physics* 53 (10): R123-R181. doi:10.1063/1.331665
- Born M. 1940. On the stability of crystal lattices. I. *Mathematical Proceedings of the Cambridge Philosophical Society*. 36: 160 – 172. doi:10.1017/S0305004100017138.
- Born M, Huang K, Lax M. 1955. Dynamical Theory of Crystal Lattices. *American Journal of Physics*, 23 (7): 474-474. doi:10.1119/1.1934059.
- Cao Y, Zhu J, Liu Y, Nong Z, Lai Z. 2013. First-principles studies of the structural, elastic, electronic and thermal properties of Ni₃Si. *Computational Materials Science* 69: 40-45. doi:10.1016/j.commatsci.2012.11.037
- Chetty N, Muoz A, Martin RM. 1989. First-principles calculation of the elastic constants of AlAs. *Physical Review B* 40 (17): 11934-11936. doi:10.1103/physrevb.40.11934.
- Chun-Lei W, Ben-Hai Y, Hai-Liang H, Dong C, Hai-Bin S. 2009. First principles study on the elastic and thermodynamic properties of TiB₂ crystal under high temperature. *Chinese Physics B* 18 (3): 1248.
- Feng L, Li N, Yang M, Liu Z. 2014. Effect of pressure on elastic, mechanical and electronic properties of WSe₂: A first-principles study. *Materials Research Bulletin*, 50: 503–508. doi:10.1016/j.materresbull.2013.11.016.
- Gehrsitz S, Sigg H, Herres N, Bachem K, Köhler K, Reinhard FK. 1999. Compositional dependence of the elastic constants and the lattice parameter of Al_xGa_{1-x}As. *Physical Review B* 60 (16): 11601–11610. doi:10.1103/physrevb.60.11601.
- Guemou M, Abdiche A, Riane R, Khenata R. 2014. Ab initio study of the structural, electronic, and optical properties of BAs and BN compounds and BN_xAs_{1-x} alloys. *Physica B: Condensed Matter* 436: 33–40. doi:10.1016/j.physb.2013.11.030.
- Güler E, Güler M. 2015. Elastic and mechanical properties of hexagonal diamond under pressure. *Applied Physics A* 11 (2): 721–726. doi:10.1007/s00339-015-9020-8.
- Guler M, Guler E. 2014. High pressure phase transition and elastic behavior of europium oxide. *Journal of Optoelectronic and Advanced Materials* 16 (11-12): 1322-1327.
- Güler E, Güler M. 2014. Phase transition and elasticity of gallium arsenide under pressure. *Materials Research* 17 (5): 1268–1272. doi:10.1590/1516-1439.272414.
- Greaves GN, Greer AL, Lakes RS, Rouxel T. 2011. Poisson's ratio and modern materials. *Nature Materials* 10 (11): 823–837. doi:10.1038/nmat3134.
- Harrison AW. 1989. *Electronic Structure and Properties of Solids*, New York: Dover.

- Hong-Lin C, Xiang-Rong C, Guang-Fu J, Dong-Qing W. 2008. Structures and Phase Transition of GaAs under Pressure. *Chinese Physics Letters* 25 (6): 2169–2172. doi:10.1088/0256-307x/25/6/067.
- Jun Z, Jing-Xin Y, Yan-Ju W, Xiang-Rong C, Fu-Qian J. 2008. First-principles calculations for elastic properties of rutile TiO₂ under pressure. *Chinese Physics B* 17(6): 2216-2221.
- Kabita K, Jameson M, Sharma BI, Brojen RK, Thapa RK. 2016. A detailed first principles study on the structural, elastic, and electronic properties of indium arsenide (InAs) under induced pressure. *Canadian Journal of Physics* 94 (3): 254–261. doi:10.1139/cjp-2015-0275.
- Li X-X, Tao X-M, Chen H-M, Ouyang Y-F, Du Y. 2013. The pressure dependences of elastic and lattice dynamic properties of AlAs from ab initio calculations. *Chinese Physics B* 22 (2): 026201. doi:10.1088/1674-1056/22/2/026201.
- Liu CG, Lu WZ, Klein MB. 1995. Pressure-induced phase transformations in AlAs: Comparison between ab initio theory and experiment. *Physical Review B* 51: 5678. doi: 10.1103/PhysRevB.51.5678.
- Louail L, Maouche D, Hachemi A. 2006. Elastic properties of InAs under pressure up to 18 GPa. *Materials Letters* 60 (27): 3269–3271. doi:10.1016/j.matlet.2006.03.011.
- Mouhat F, Coudert F-X. 2014. Necessary and sufficient elastic stability conditions in various crystal systems. *Physical Review B* 90 (22): 4104. doi:10.1103/physrevb.90.224104.
- Na-Na L, Ren-Bo S, Da-Wei D. 2009. Elastic constants and thermodynamic properties of Mg₂SixSn_{1-x} from first-principles calculations. *Chinese Physics B* 18 (5): 1979.
- Pokluda J, Černý M, Šob M, Umeno Y. 2015. Ab initio calculations of mechanical properties: Methods and applications. *Progress in Materials Science*, 73: 127-158. doi: 10.1016/j.pmatsci.2015.04.001.
- Pugh SF. 1954. Relation between the elastic moduli and the plastic properties of polycrystalline pure metals. *Philosophical Magazine and Journal of Science* 45 (367): 823–843. doi:10.1080/14786440808520496.
- Rahmati A, Ghoohestani M, Badehian H, Baizae M. 2014. Ab. initio study of the structural, elastic, electronic and optical properties of Cu₃N. *Materials Research* 17 (2): 303-310. doi: 10.1590/s1516-14392014005000039 .
- Varshney D, Joshi G, Varshney M, Shriya S. 2010. Pressure dependent elastic and structural (B3–B1) properties of Ga based mononictides. *Journal of Alloys and Compounds* 495 (1): 23–32. doi:10.1016/j.jallcom.2010.01.077.
- Venkateswaran UD, Cui LJ, Weinstein BA, Chambers FA. 1992. Forward and reverse high-pressure transitions in bulklike AlAs and GaAs epilayers. *Physical Review B* 45(16): 9237–9247. doi:10.1103/physrevb.45.9237.
- Wang S, Li, J-X, Du Y-L, Cui C. 2014. First-principles study on structural, electronic and elastic properties of graphene-like hexagonal Ti₂C monolayer. *Computational Materials Science*, 83: 290–293. doi:10.1016/j.commatsci.2013.11.025.
- Zi-Jiang L, Jian-Hong Q, Yuan G, Qi-Feng C, Ling-Cang C, Xiang-Dong Y. 2007. Thermoelasticity of CaO from first principles. *Chinese Physics* 16 (2): 499-505. doi: 10.1088/1009-1963/16/2/035.